

Math 107

Spring 2017

Lecture 2

Ch. 2 : Basic Percent

① By translation

② By Proportion

what, what number

x

p%, what percent

$\frac{p}{100}$

% of

\cdot

is, get, become, equal

$=$

a of b

$\frac{a}{b}$

what is 4% of 250?

$$\begin{array}{c} \downarrow \quad \downarrow \quad \downarrow \\ x = \frac{4}{100} \cdot 250 \end{array}$$

$$x = .04 (250)$$

$$x = 10$$

4% of 250 is 10.

10 is 4% of 250.

8% of what number is 400?

$$\frac{8}{100} \cdot x = 400$$

$$.08 \cdot x = 400$$

$$.08x = 400$$

$$x = \frac{400}{.08} \Rightarrow x = 5000$$

8% of 5000 is 400.

What Percent of 250 is 750?

$$\frac{P}{100} \cdot 250 = 750$$

$$\frac{\cancel{250}^{25}}{\cancel{100}^{10}} P = 750$$

$$\frac{25}{10} P = 750$$

$$2.5 P = 750$$

$$P = \frac{750}{2.5}$$

$$P = 300$$

300% of 250
is 750.

What Percent is 3 of 8?

$$\frac{P}{100} = \frac{3}{8}$$

Multiply both sides by 100

$$\cancel{100} \cdot \frac{P}{\cancel{100}} = 100 \cdot \frac{3}{8}$$

$$P = \frac{300}{8}$$

$$P = 37.5$$

37.5% is 3 of
8.

4.5% of what number is 150?

$$\frac{4.5}{100} \cdot x = 150$$

$$.045 x = 150$$

$$.045 x = 150$$

$$x = \frac{150}{.045} \quad x = 3333.\bar{3}$$

About 4.5% of 3333 is 150.

120% of what number is 600?

$$\frac{120}{100} \cdot x = 600$$

$$\frac{12}{10} x = 600$$

$$1.2 x = 600$$

$$x = \frac{600}{1.2}$$

$$x = 500$$

120% of 500 is 600

A computer is on sale @ 20% off.

the Sale price is \$680.

find the original price.

we are paying
80% of original
Price.

80% of original price is the Sale price.

$$\frac{80}{100} \cdot x = 680 \quad \rightarrow \quad x = \frac{680}{.8}$$

$$x = 850$$

$$.8x = 680$$

$$\boxed{\$850}$$

Lisa works at a dealership and gets Paid by Commission. Her Salary is 4% of her sales.

Last month, her salary was \$2800.

find the amount of her sale.

4% of her sale is her salary

$$\frac{4}{100} \text{ of } x = 2800$$

$$.04 \cdot x = 2800$$

$$x = \frac{2800}{.04}$$

$$\rightarrow x = 70,000$$

her sale was
\$70,000

Due
Next

week: wp ch.2

Ratio of a to b is $\frac{a}{b}$

Ratio of 1.5 to 45 is $\frac{1.5}{45}$

$$\frac{1.5}{45} = \frac{1.5(10)}{45(10)} = \frac{15}{450} = \frac{\cancel{15} \cdot 1}{\cancel{15} \cdot 30} = \frac{1}{30}$$

1.5 cups of Sugar for 20 Muffins.

$$\frac{1.5 \text{ cups Sugar}}{20 \text{ Muffins}}$$

How many cups of Sugar for 50 Muffins.

$$\frac{x \text{ cups of Sugar}}{50 \text{ Muffins.}}$$

If we equate two ratios, we get
Proportion.

$$\frac{1.5}{20} = \frac{x}{50}$$

To Solve a proportion, we cross-Multiply

$$20x = 50(1.5)$$

$$x = \frac{50(1.5)}{20}$$

$$x = 3.75$$

3.75 cups of sugar for 50 muffins.

2.5 inches on the map is for 400
actual miles.

Two cities were 8 inches apart on the map.

Find actual distance.

$$\frac{2.5 \text{ inches}}{400 \text{ Miles}} = \frac{8 \text{ inches}}{x \text{ Miles}}$$

$$\frac{2.5}{400} = \frac{8}{x}$$

$$2.5x = 8(400)$$

$$x = \frac{8(400)}{2.5}$$

$$x = 1280$$

Actual distance is
1280 miles.